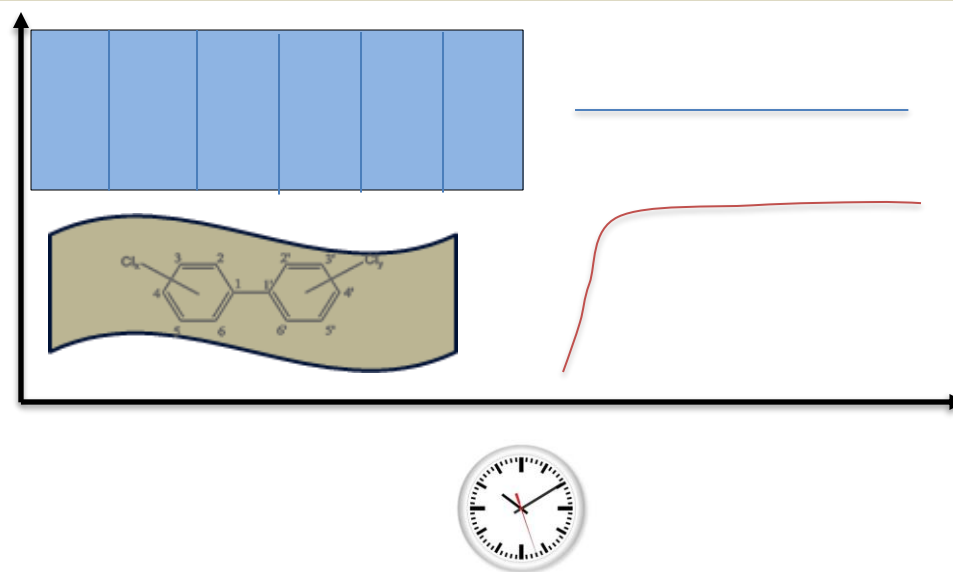
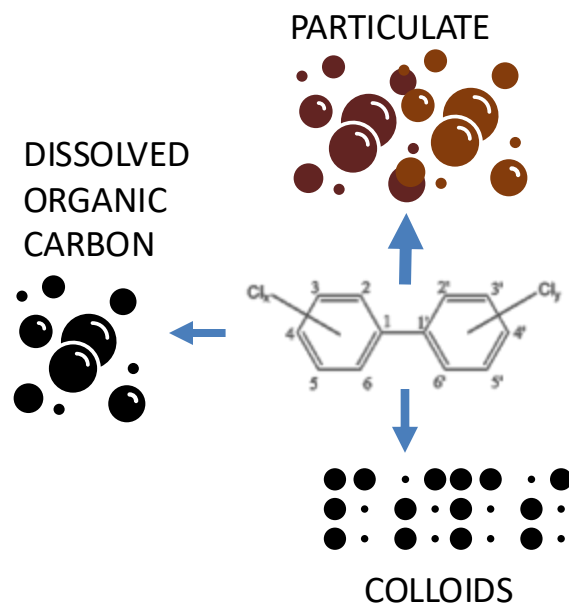


# How Efficient is Time-Integration for Equilibrium Passive Sampling?

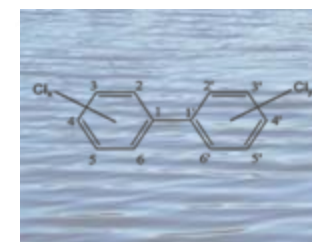


**Oindrila Ghosh, Songjing Yan, Mandar Bokare, Upal Ghosh**

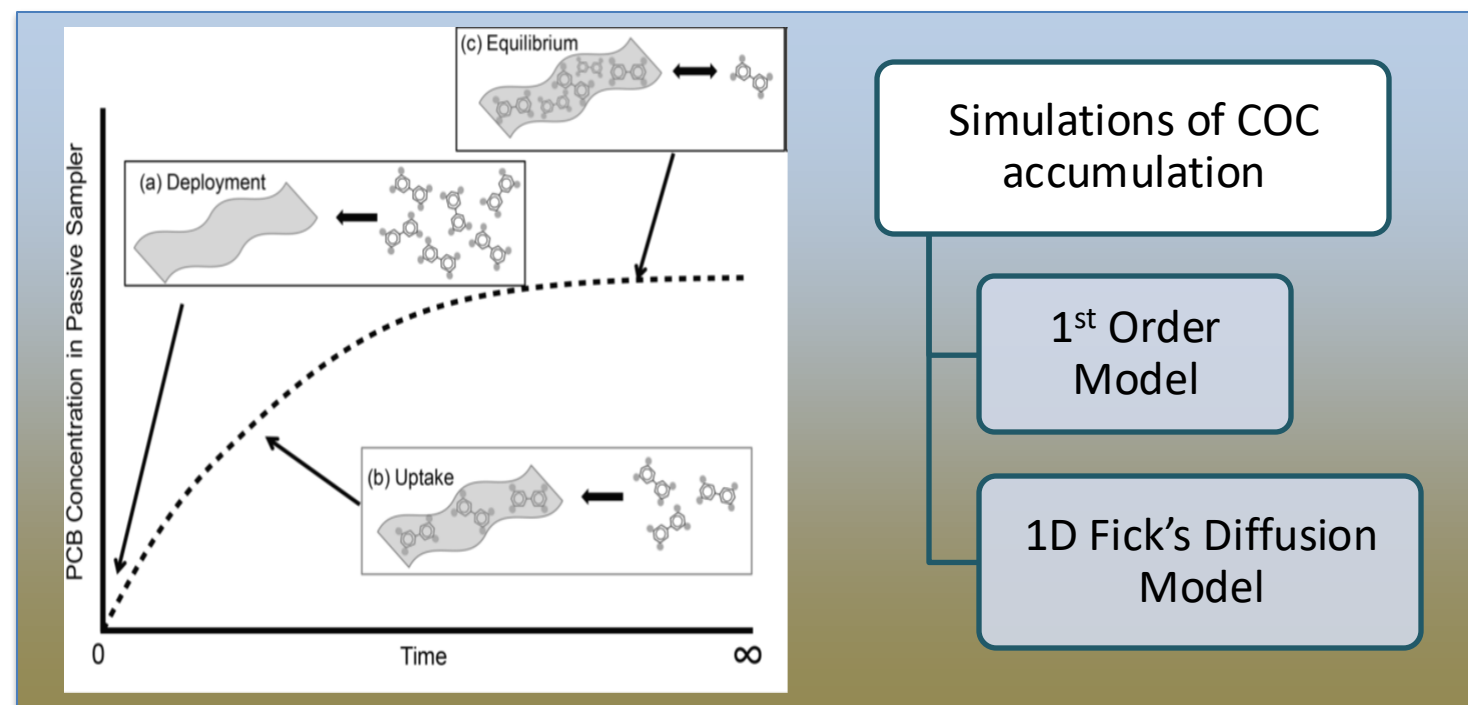
Department of Chemical, Biochemical and Environmental Engineering,  
University of Maryland Baltimore County



FREELY DISSOLVED  
CONCENTRATION  
(bioavailable)

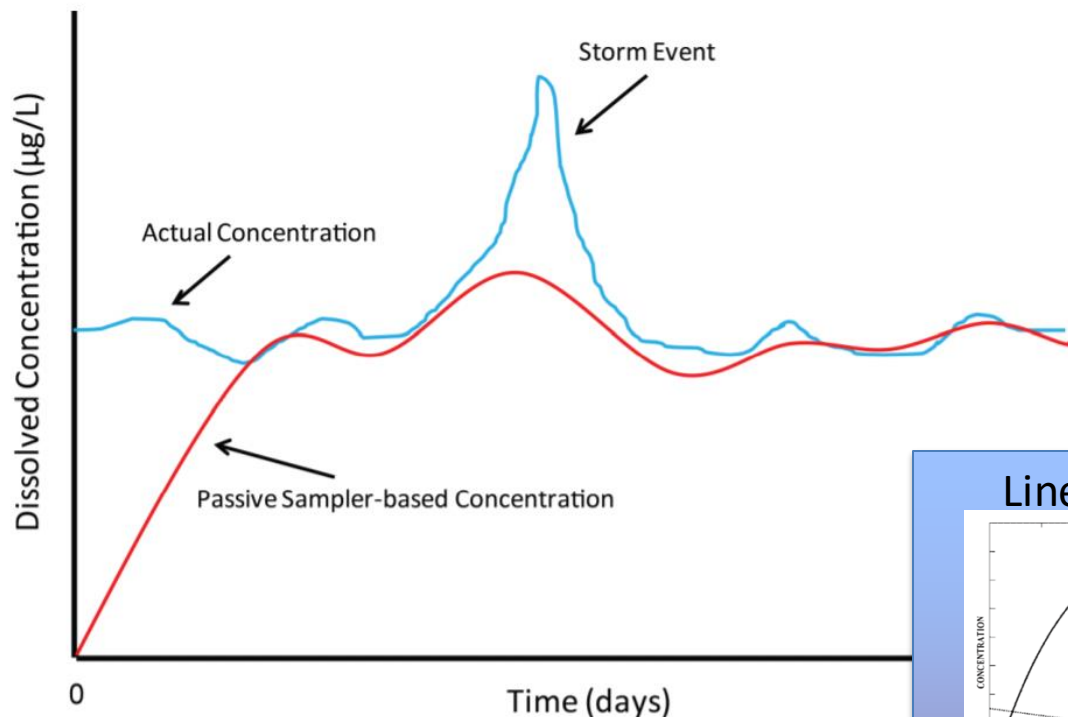


Freely dissolved conc. of contaminant in  
water column/ interstitial water (ug/L)  
[Ghosh et al., 2014]

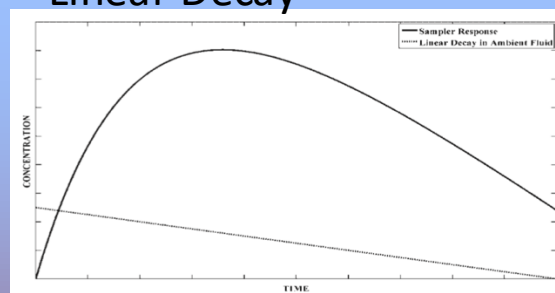


## AIM

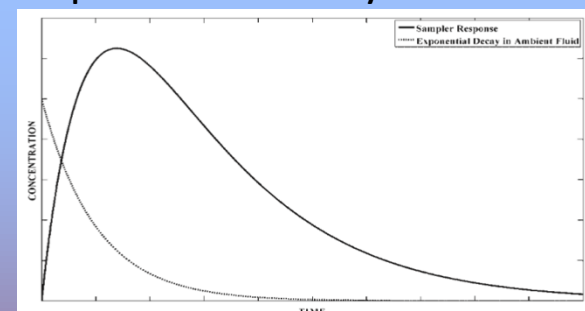
- In the real environment, water concentrations of these HOCs vary temporally.
- Important for ecological exposure assessment.
- **How well passive sampler concentrations represent the time-averaged concentration over an entire deployment period?**



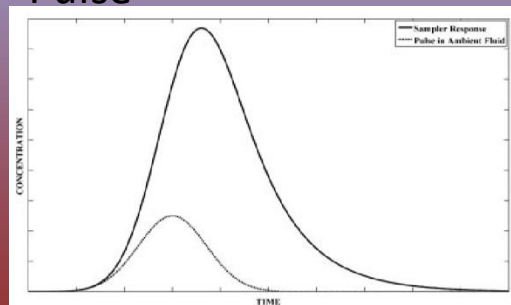
### Linear Decay



### Exponential Decay



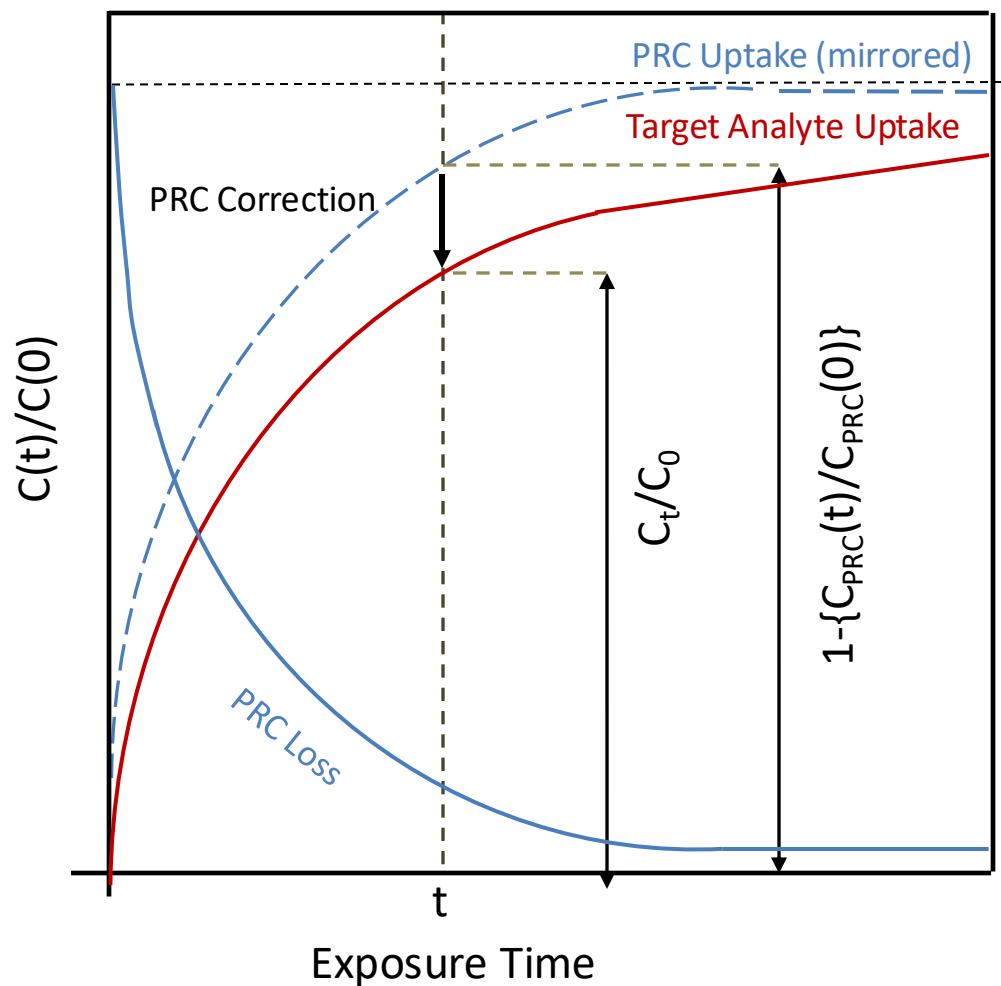
### Pulse



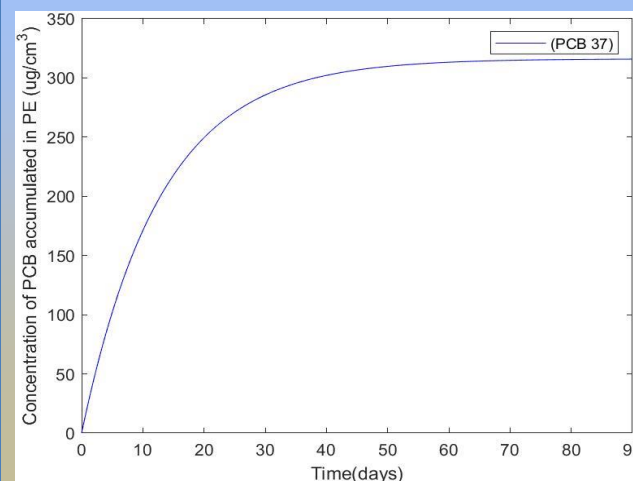
- Characteristic of ambient concentration
- Passive sampler-based water concentration (Analytical solution)

Hawker et al., 2009

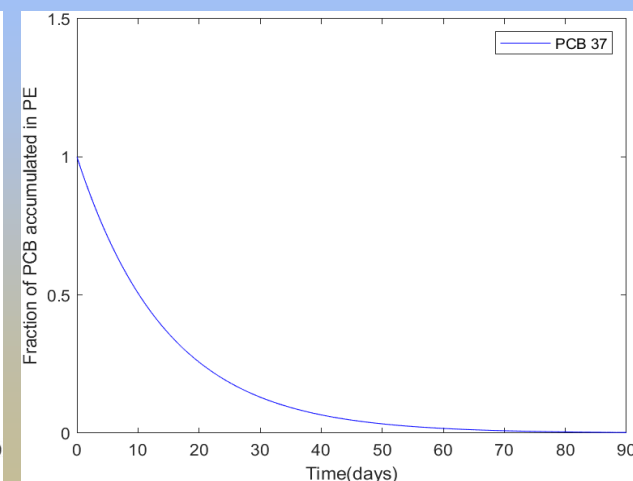
## PERFORMANCE REFERENCE COMPOUND CORRECTION FOR EQUILIBRIUM



**Gain Function =  
Actual Mass Gained**



**Loss Function =  
Fraction of Loss**



$$\text{Corrected Mass of PCB Uptake} = \frac{\text{Actual Mass Gained}}{\text{Fraction of Loss}}$$

$$C_w = \frac{\text{Corrected Mass of PCB Uptake}}{K_{PEW}}$$

**INITIAL CONDITIONS: Water concentration varies  
from 1ng/L to 0.1ng/L.**

## FIRST ORDER MODEL

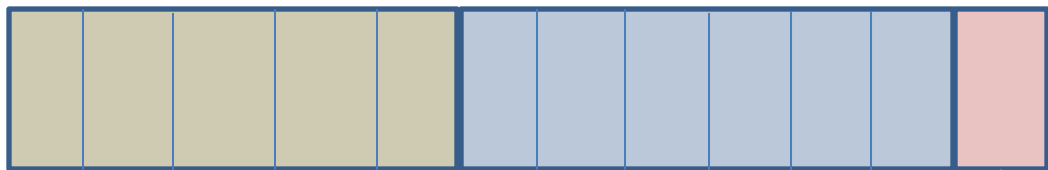
### Governing Equation:

Calculation of Mass of PCB accumulated in PE ( $C_{PE}$ )

$$\frac{dC_{PE}}{dt} = k_u C_W - k_e C_{PE}$$

Calculation of Mass of PCB accumulated in PE  
at Equilibrium ( $C_{PE\_Eq}$ )

$$C_{PE\_Eq} = C_{PE} / (1 - e^{-k_e T})$$



Eq 1

Eq 3

Eq 2

CoinW; infinite  
bath no flux  
boundary  
condition.

## FICK'S DIFFUSION MODEL

### Governing Equation: System of well mixed infinite water bath

Eq 1 
$$\frac{\partial C_{PE}}{\partial t} = D_{PE} \frac{\partial^2 C_{PE}}{\partial x^2} \quad \text{for } -l < x < l$$

Eq 2 
$$\frac{\partial C_W}{\partial t} = D_W \frac{\partial^2 C_W}{\partial x^2} \quad \text{for } -l > x > -(l+b) \text{ and } l < x < (l+b)$$

### Boundary Conditions:

At the interface of the PE and water, the diffusive fluxes match so that mass is conserved

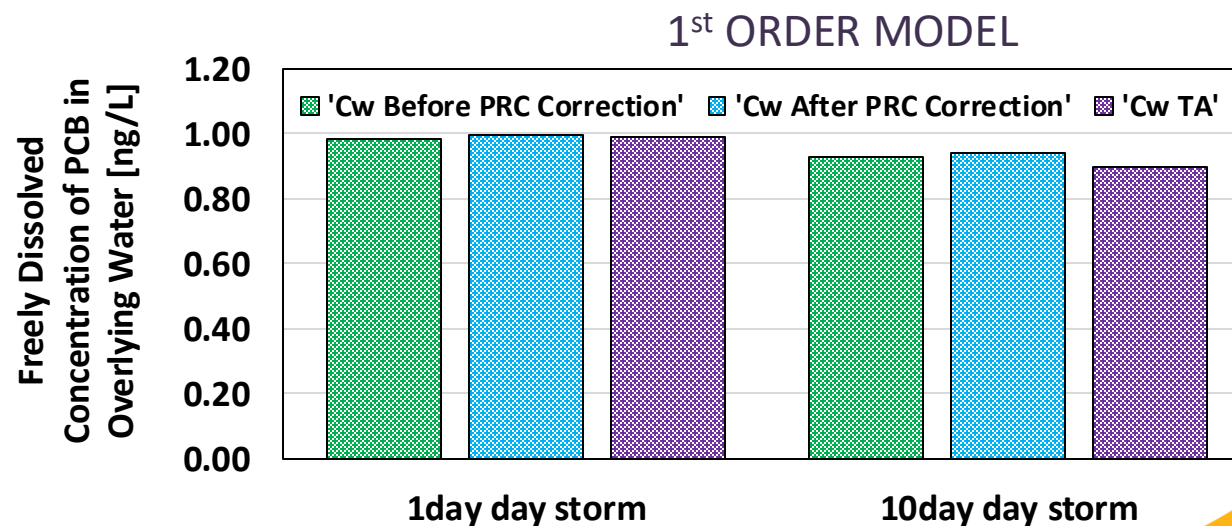
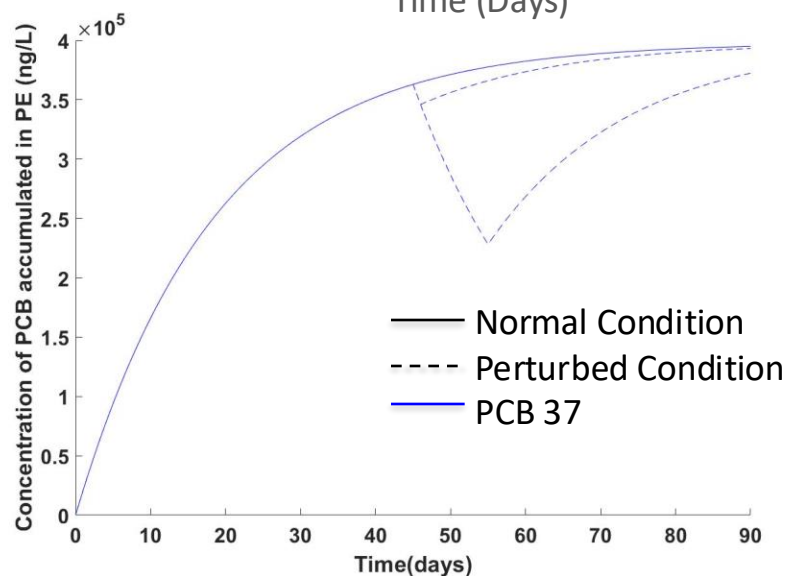
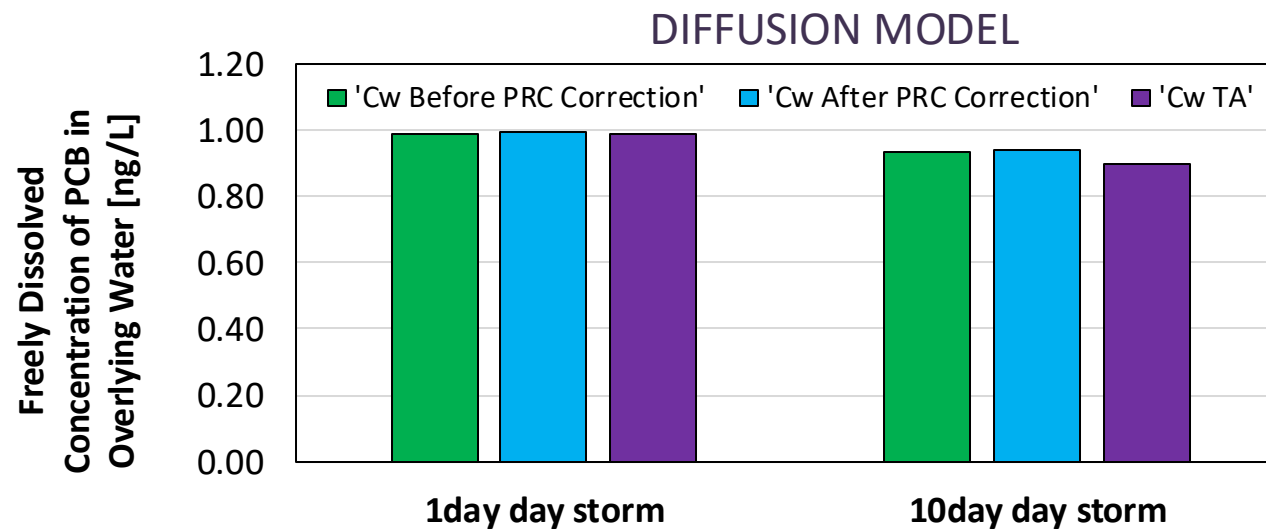
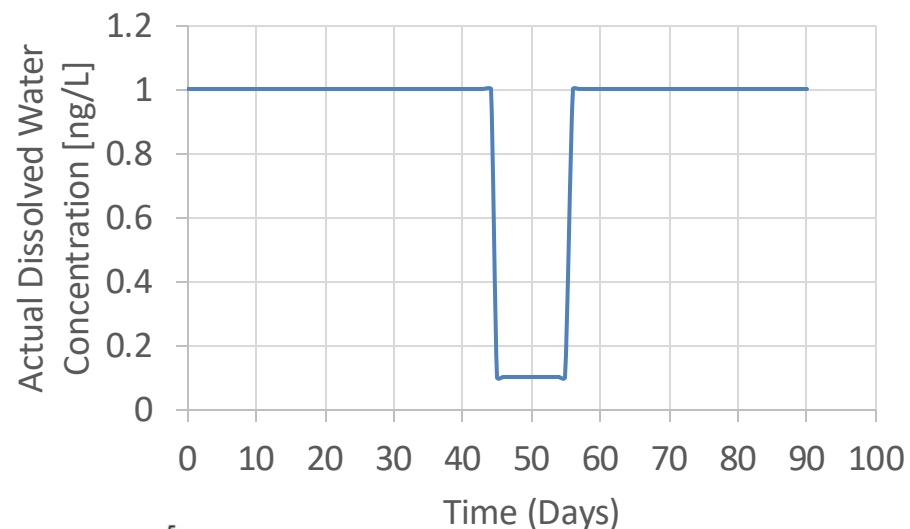
$$D_{PE} \frac{dC_{PE}}{dx} = D_W \frac{dC_W}{dx} \quad \text{for } x = l \text{ and } x = -l$$

local equilibrium distribution

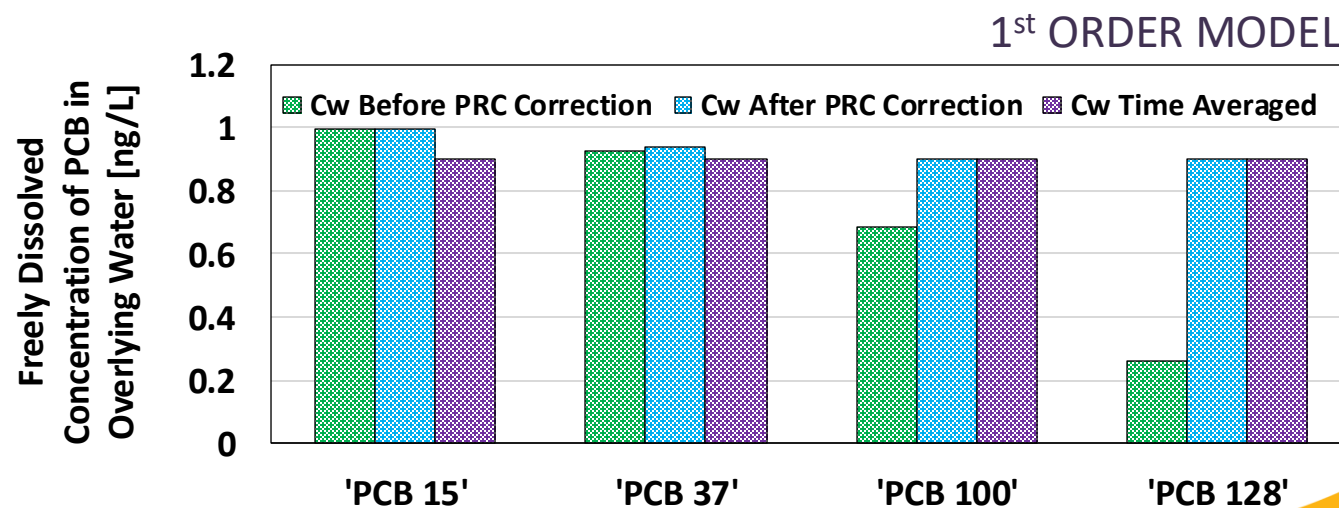
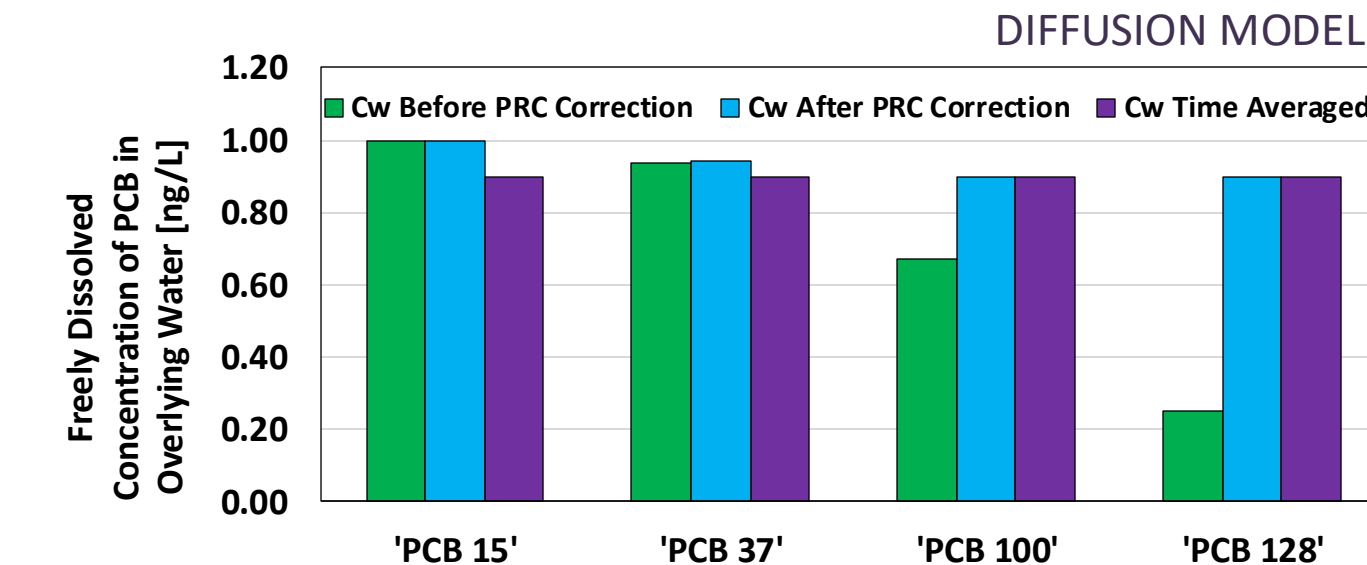
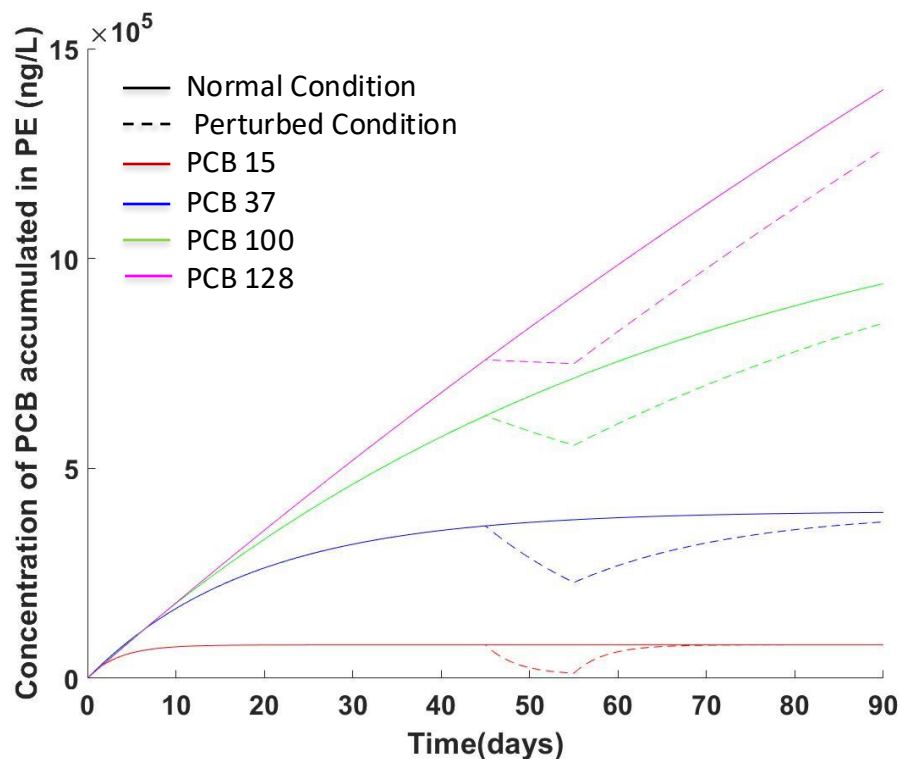
$$C_{PE} = K_{PEW} C_W \quad \text{at } x = l \text{ and } x = -l$$

Eq 3

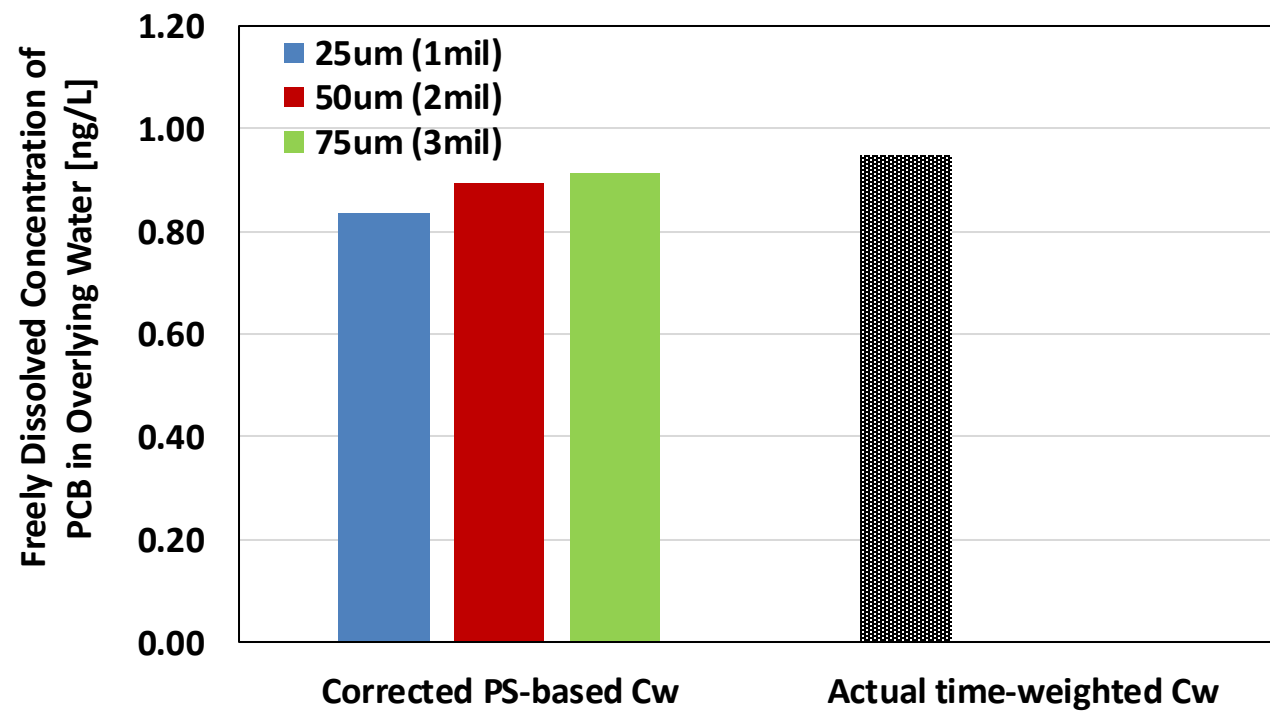
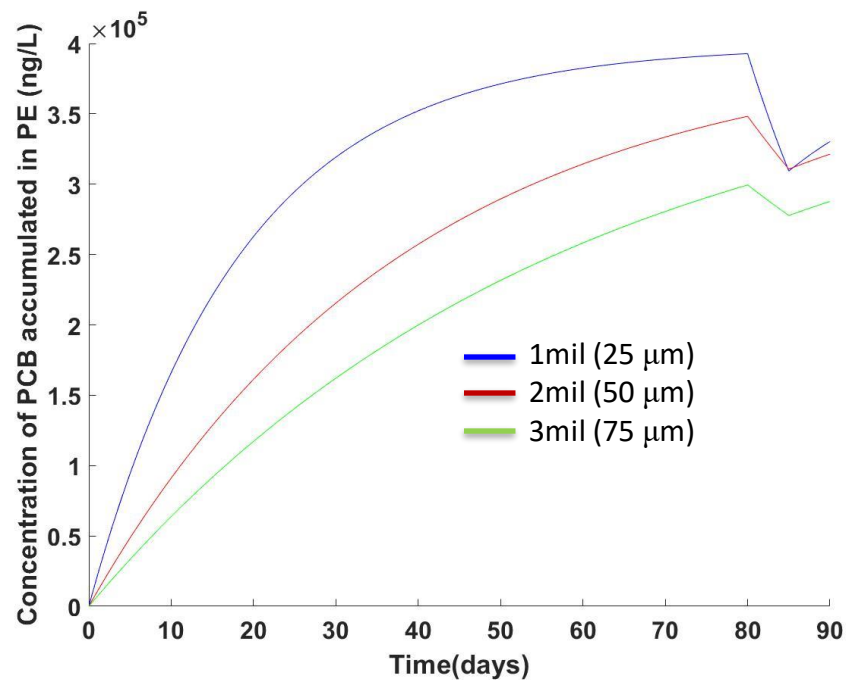
## Impact of a 10-day long perturbation on the uptake of PCB 37



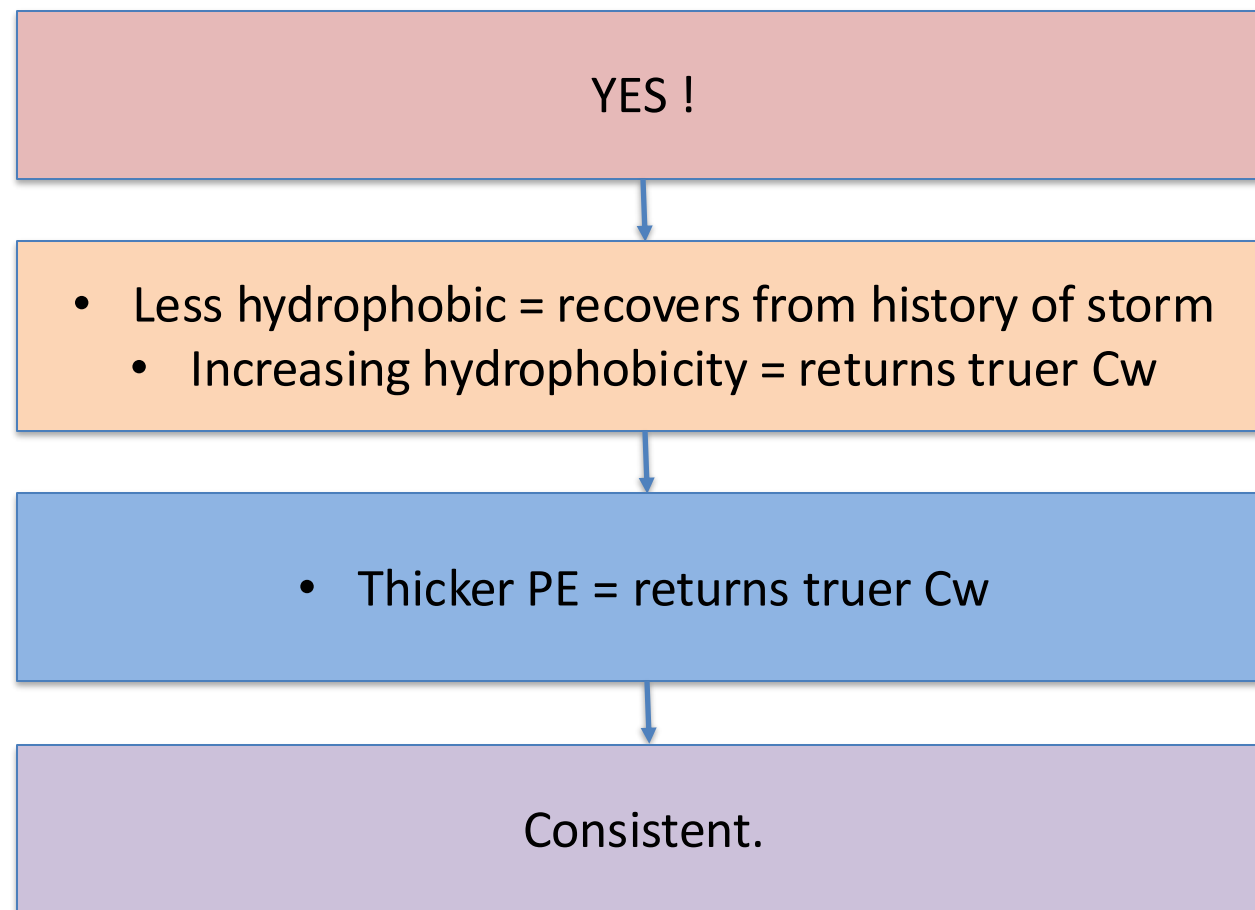
## Effect of 10-day long perturbation on the uptake of different PCB homologs



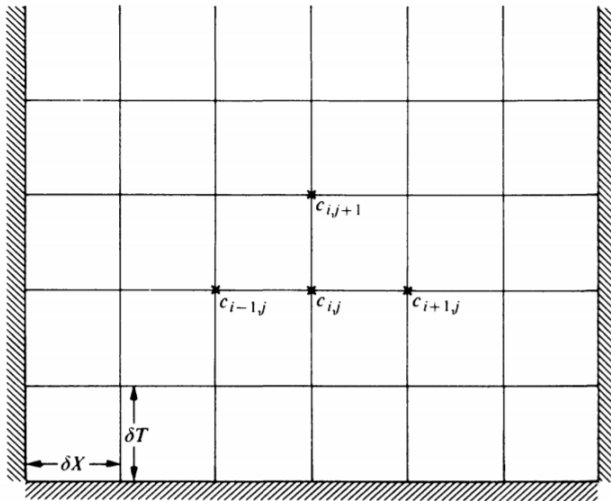
## Impact of various PE thickness on the uptake of PCB 37



- Is there a time period beyond which a perturbation in concentration is not captured in the passive sampling time-integration?



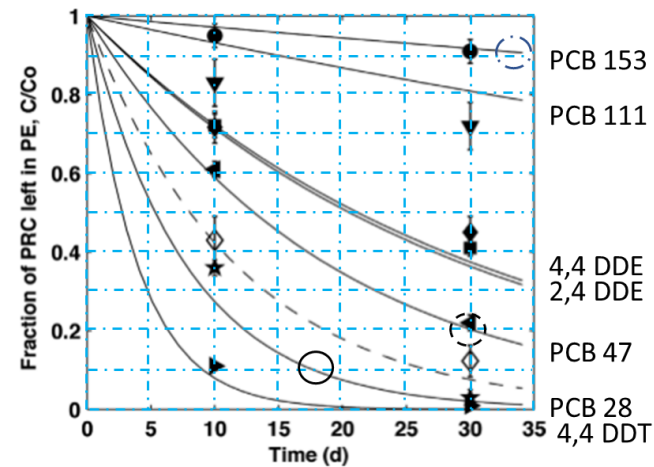
THANK YOU



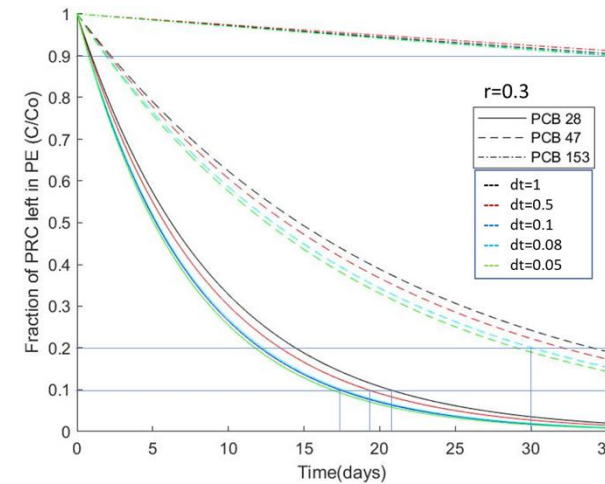
$$c_{i,j+1} = c_{i,j} + r(c_{i-1,j} - 2c_{i,j} + c_{i+1,j}),$$

$$r = \delta T / (\delta X)^2. \quad r < 0.5$$

Analytical solution in  
Tcacuic et al, 2015



Our Model



[wbl:0.02cm, 25um PE;  
Infinite Water Bath]

[r=0.3; dt=0.1s]

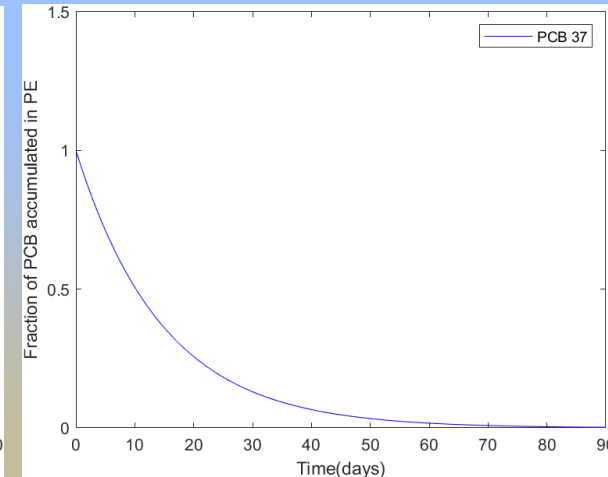
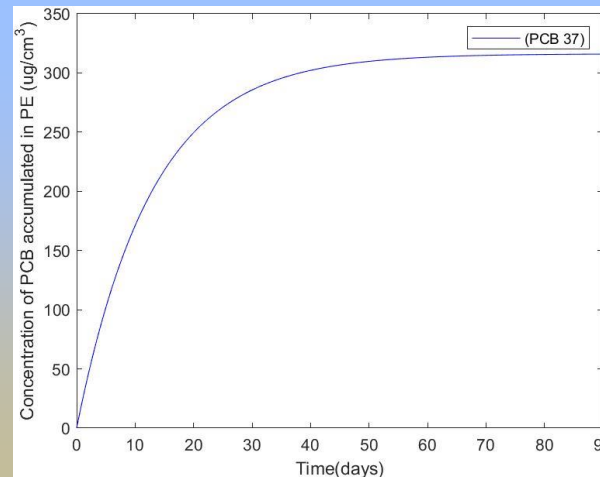
## INITIAL CONDITIONS:

### 1. NO STORM CONDITION

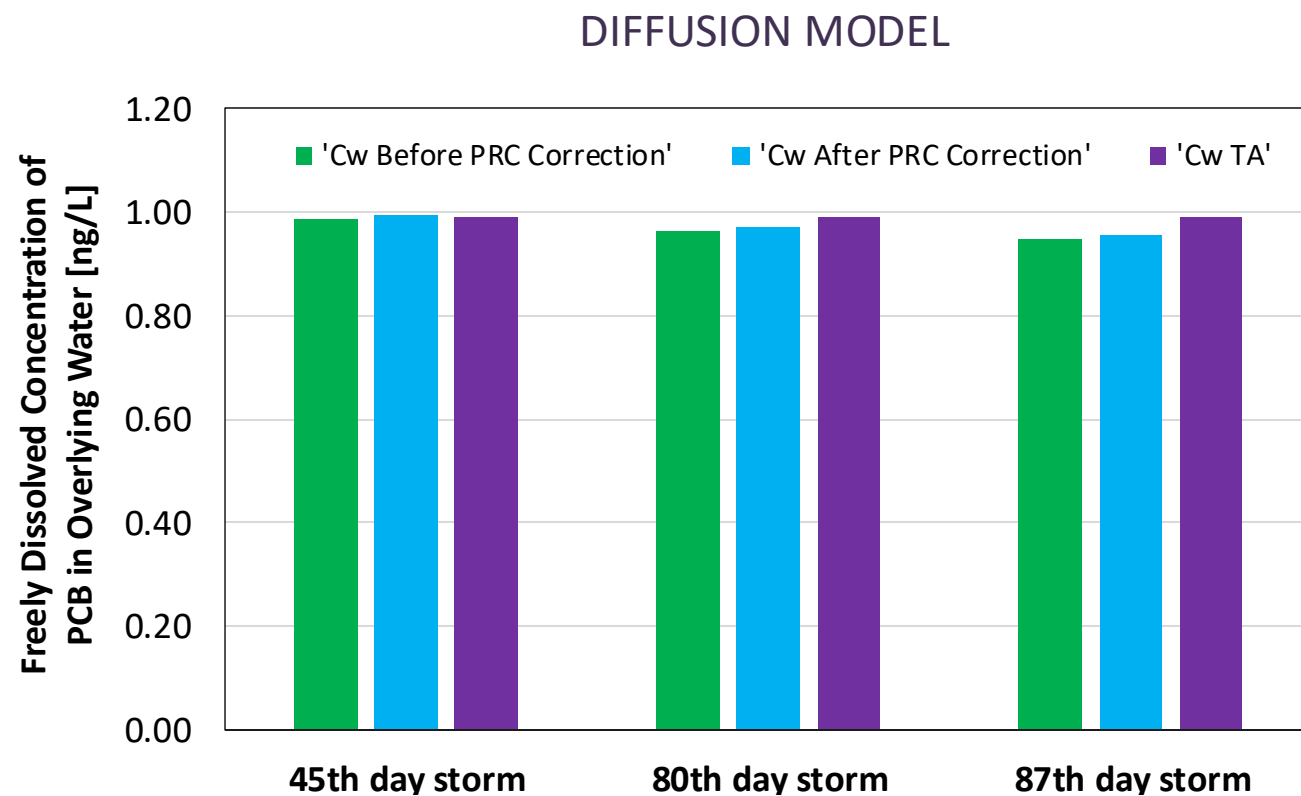
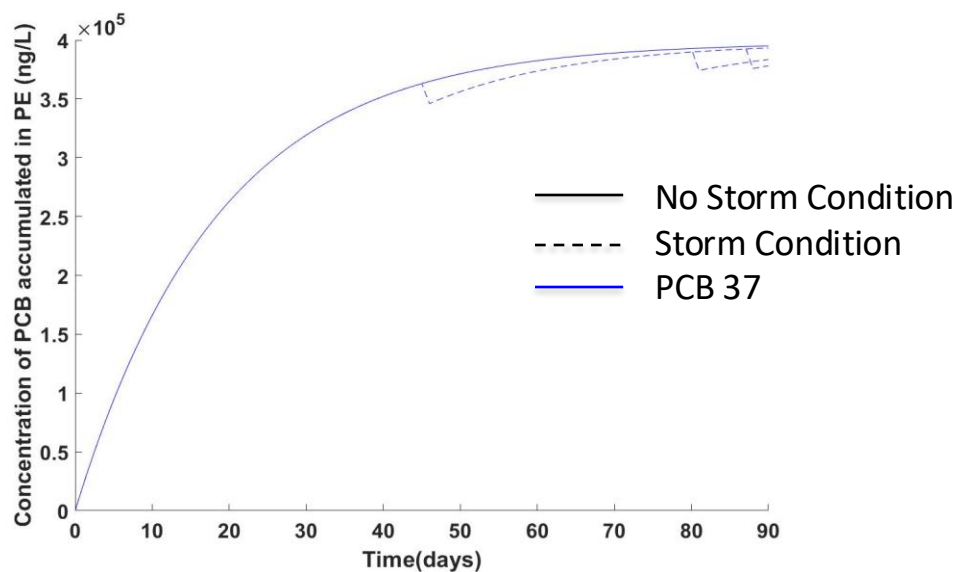
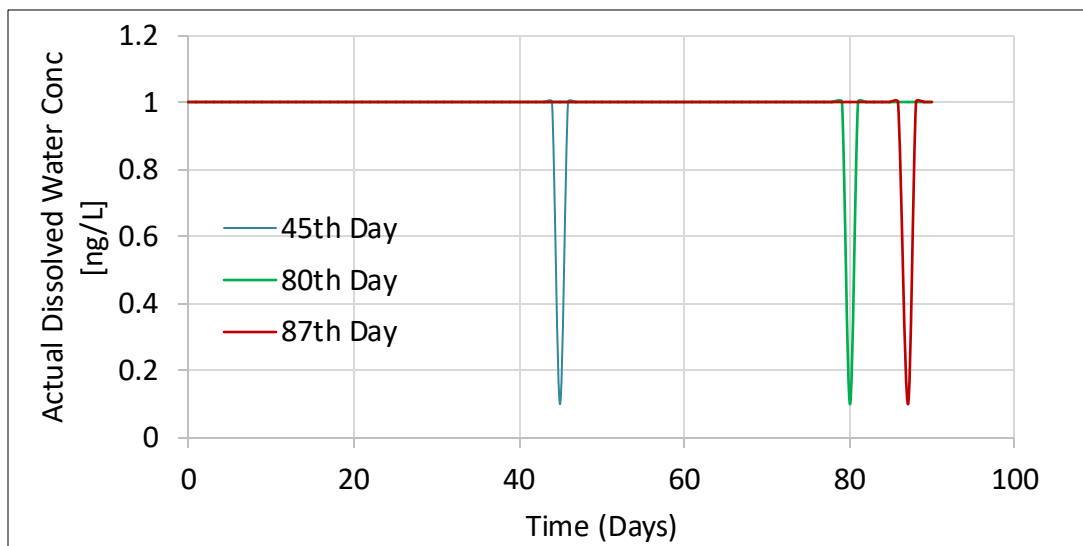
- Water: 1 ng/L
- PE: 0 ng/L

### 2. Storm

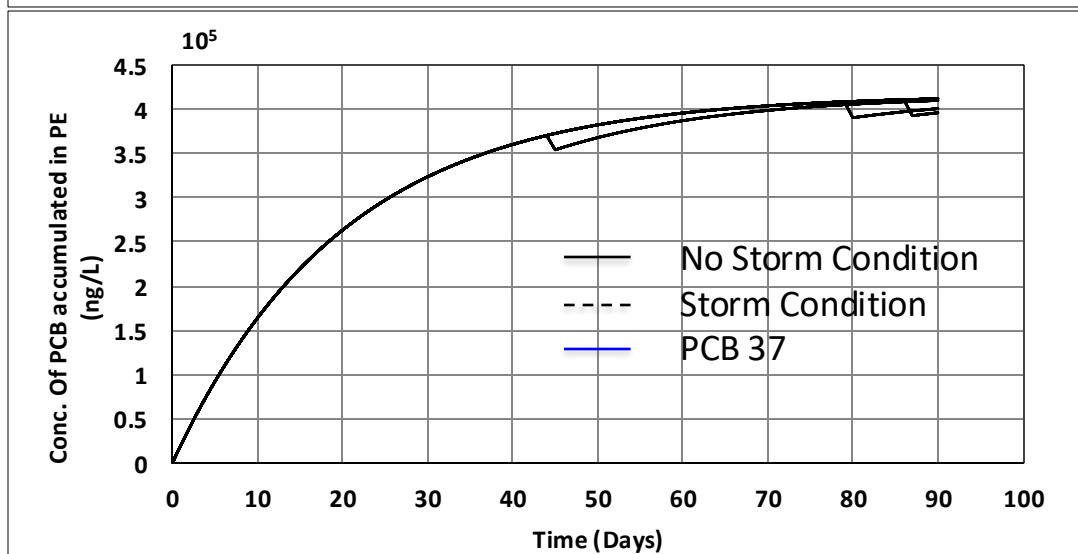
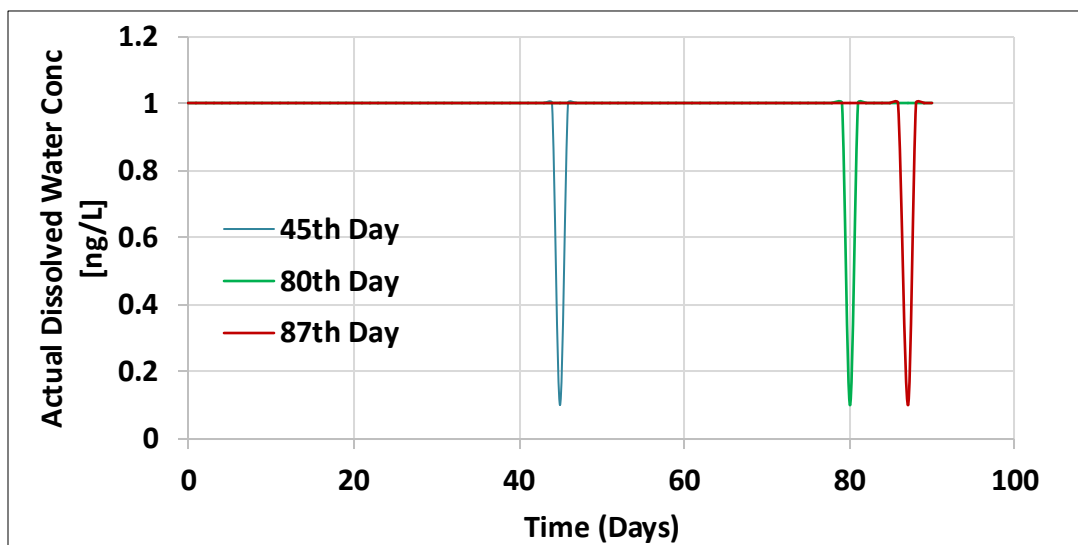
- Water: 0.1ng/L



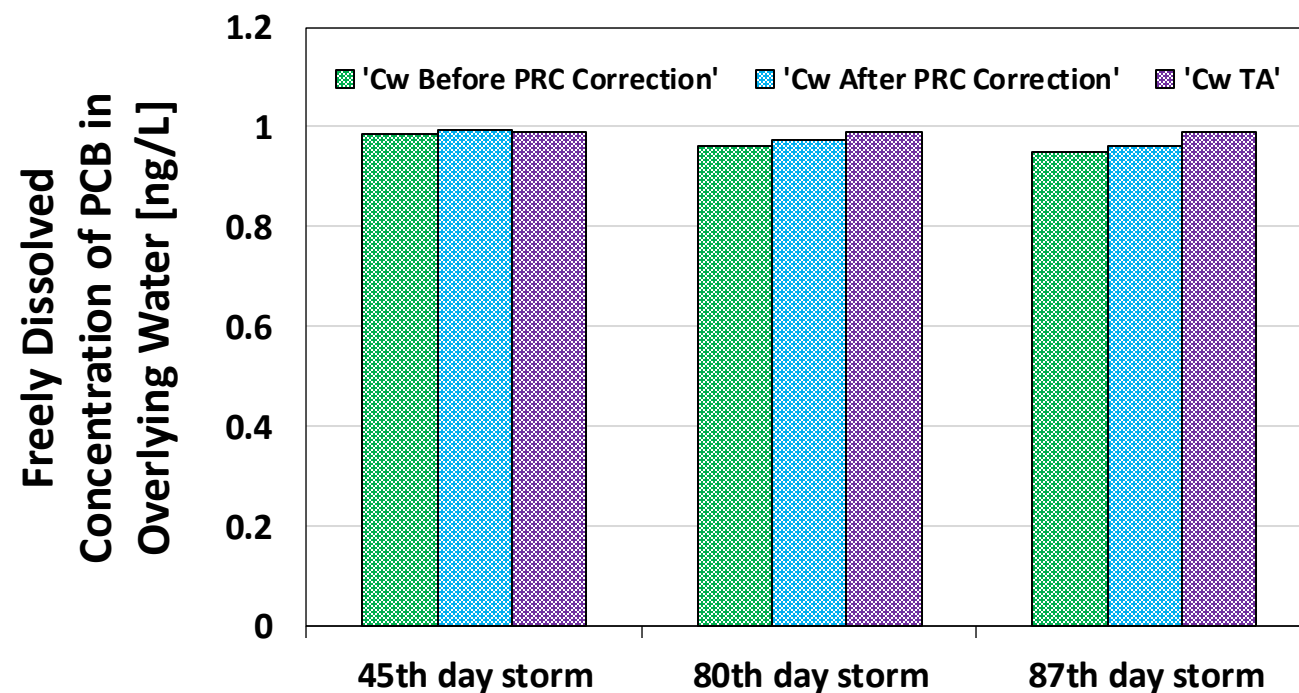
Impact of 1-day long storms on different days during the deployment period on the uptake of PCB 37



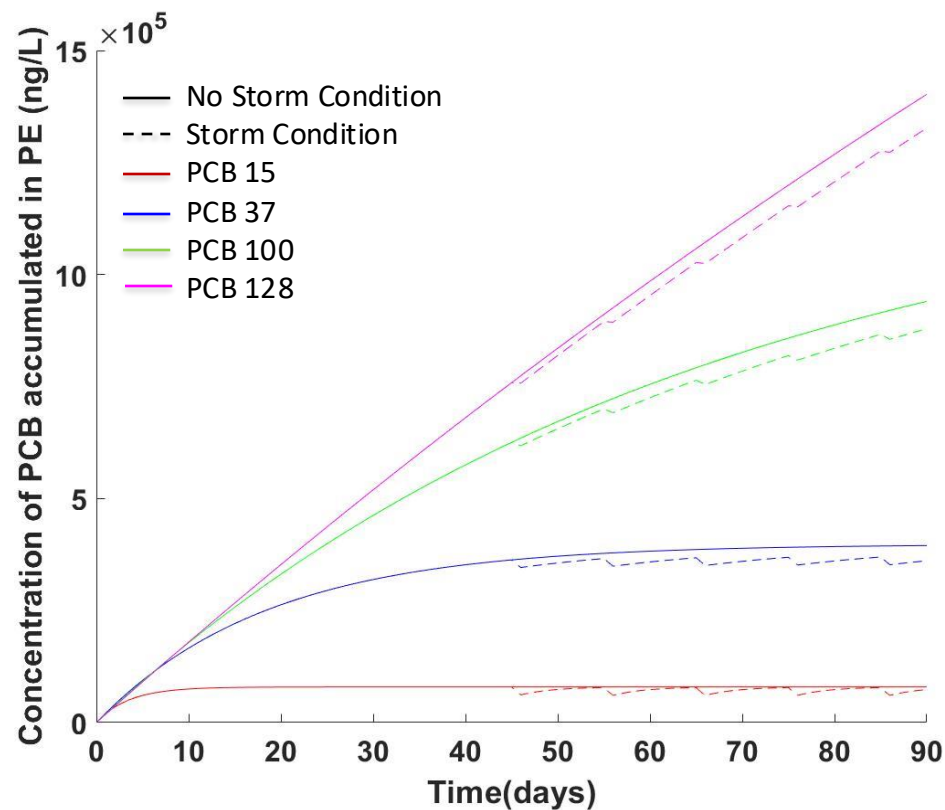
Impact of 1-day long storms on different days during the deployment period on the uptake of PCB 37



## 1<sup>st</sup> ORDER MODEL



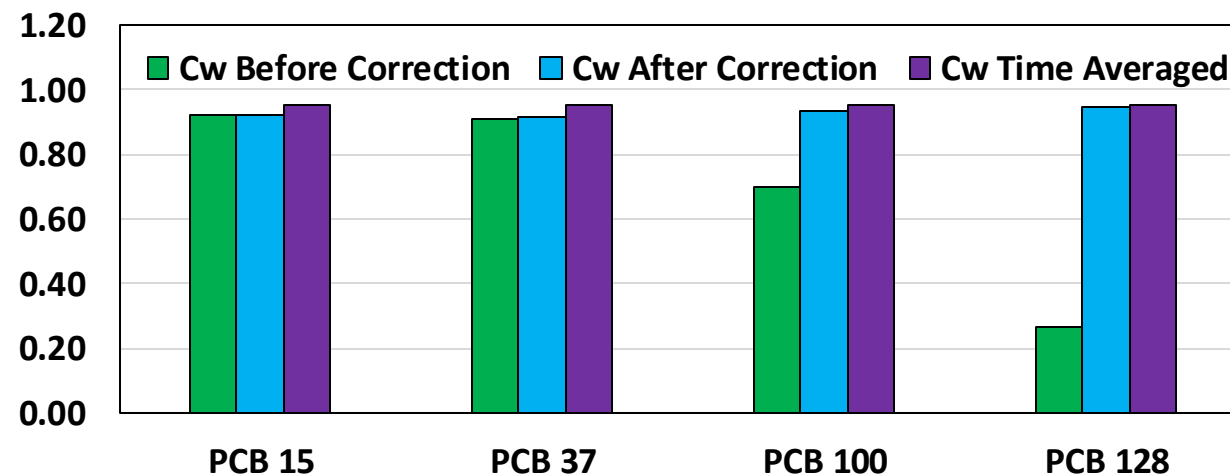
## Impact of Periodic Storms on the Uptake of Various Homologs



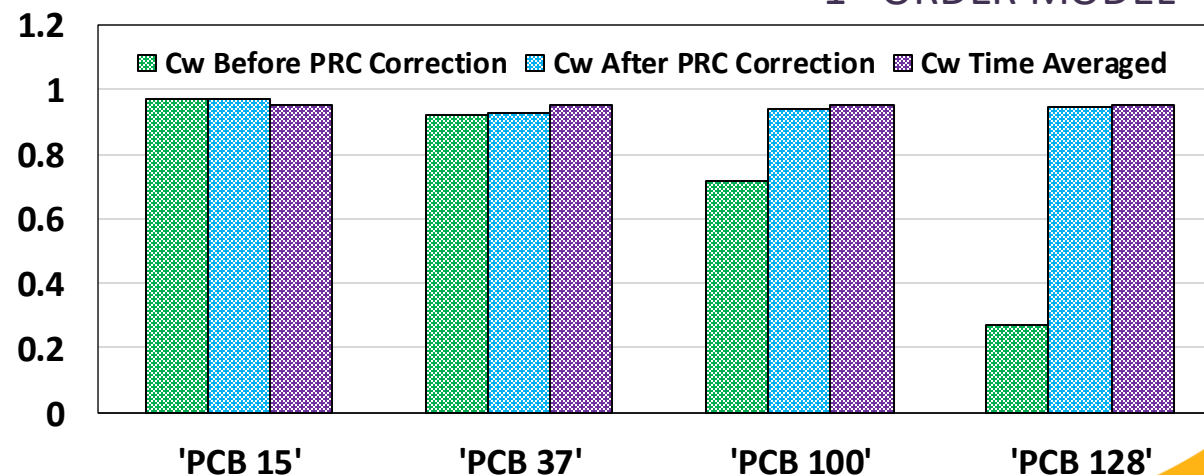
Freely Dissolved  
Concentration of PCB in  
Overlying Water [ng/L]

Freely Dissolved  
Concentration of PCB in  
Overlying Water [ng/L]

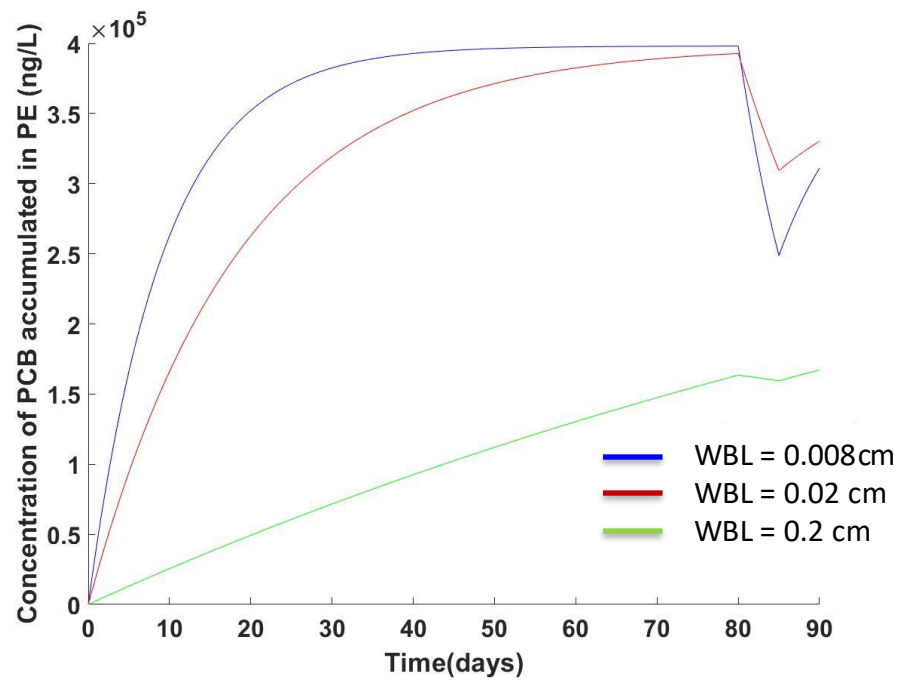
### DIFFUSION MODEL



### 1<sup>st</sup> ORDER MODEL



## Impact of Varying Water Boundary Layer (WBL) Thickness on the Uptake of PCB 37



Freely Dissolved Concentration of PCB in Overlying Water [ng/L]

